Is Online Trading Gambling with Peanuts?

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Abstract

If individuals derive a small utility from gambling, we should observe high turnover in portfolios that are of only marginal importance to them. By the use of detailed individual financial data, as well as trades from a Swedish online broker, I measure the frequency and cost of online trading in the cross-section, and find the opposite relation. Those who have online portfolios that constitute a large share of risky assets trade more aggressively, but have lower trading performance. These results can be explained by a simple Treynor-Black portfolio model where investors suffer from biased self-assessment, rather than possessing true investment skill. The overall result suggests that the cost of online trading can be substantial. The top quintile of investors who have the highest share of their total financial assets in stocks invested at the brokerage firm under study loose 3.70% of their financial wealth annually, which corresponds to 1.38% of aggregate income within this group. These investors do not only have lower overall wealth and income, but also have the highest aggregate trading losses. Therefore, trading losses are mainly carried by those who can afford them the least. Across individuals, annual losses for 36% of investors exceed 1% of their financial wealth, and 17% lose more than 5%.

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1 Introduction

It is an established fact in the theory of decision making that individuals behave differently to small versus large sized gambles. Markowitz (1952b) notes that most individuals are risk seeking or neutral for small-stake gambles, say choosing a 10% chance of winning \$10 over a \$1 for certain. However, as stakes are increased, most people find it less attractive to gamble, and very few would choose a risky 10% chance of winning \$1,000,000, faced with a certain \$100,000. Prelec and Loewenstein (1991) dub this phenomena the "peanuts effect". The results from small-sized bets are difficult to interpret, as people may be simply indifferent to small stakes, or "peanuts". Conlisk (1993) suggests that individuals derive some positive utility from gambling itself that, locally, can dominate risk aversion. One would then expect people to always gamble with peanuts, but then it is unclear what the welfare implications are and how important the problem is for economic analysis. Shiller (1998) points out that the enjoyment of gambling is usually confined to specific areas, or favorite games, where individuals feel that they are especially skillful or lucky.

Investing in financial markets is very different from gambling – at least in theory. Standard, normative advise is to avoid high trading costs and hold diversified portfolios. In direct contradiction stand the two most important stylized facts in the literature of investor behavior: investors trade too much, as evidenced by Barber and Odean (2000)), and they hold poorly diversified portfolios, as documented by Goetzmann and Kumar (2005) and Polkonichenko (2004)). Kumar (2005) finds that investors with similar socioeconomic background as those preferring lottery-tickets also prefer stocks with positively skewed payoffs (e.g. poor, less educated men, living in urban areas). Given the low diversification and high trading frequency, it is only natural to ask if poor trading performance really is economically important to investors, or if it is to be regarded as some form of entertainment.

This paper aims to document to which extent trading is related to significant amounts

for individuals. The peanuts effect can be explained by individuals deriving some small, constant utility from gambling that dominates risk-aversion. This implies that it is mainly those who have proportionally small amounts of their wealth invested in their online portfolios who trade. As an alternative hypothesis, I present a portfolio choice problem with overconfidence that gives the opposite prediction. Investors who believe that they are better traders, allocate a higher share of financial assets to their traded portfolio. This is a much sharper test of overconfidence than found in most other studies, because it gives a strong cross-sectional prediction. People who trade more will do so with higher stakes, even if they are no better traders than other investors. The two features taken together directly implies that utility losses from trading can be substantial.

Unlike other performance studies, this paper makes explicit use of trading data from an online broker, as well as detailed individual financial tax reports in order to answer these questions. The *active weight* proxies for the investors belief in their trading capability, and is defined as each individuals stock portfolio value at the broker account divided by the value of all risky assets (financial wealth excluding holdings of cash and money market funds), measured at first year-end of trading. The cumulative distribution of the active portfolio for the 10,600 investors in sample is displayed in Figure 1, normalized either by risky assets or total financial assets. As expected, online portfolios constitute a relatively small part of financial wealth for many people. Around 25% of the individuals have stocks worth 5% or less of their total financial assets; around 50% of the investors 20% or less. For 50% of the individuals, the online portfolio weight of risky assets is less than 34%, which means that these investors hold more than 76% of their risky assets in other financial instruments than stocks at the online broker. At the top of the distribution, 17% of the investors have 75% or more of their financial wealth invested into stocks at the online account, and this constitute all of their holdings in risky assets. These results show that there is a wide dispersion of how much trading can effect investors utility, even if returns from trading were constant.

If losses from trading are mainly associated with "unimportant" portfolios at the left

side of Figure 1, the documented results on trading performance can be seriously misleading. To the contrary, it is found that investors with a larger share of their wealth at stake (at the right side of Figure 1) are both more likely to trade, and have a higher turnover when they do trade. There is also a negative relationship between investors' online portfolio weight and trading performance. In regressions that control for turnover, as well as portfolio size, wealth, diversification, financial occupation, risk, age, and gender it is found that the main channel for this underperformance is through increase trading, and not lower average trading ability. The results adds evidence to the previous literature on investor behavior and overconfidence, since it is shown not only that investors who trade more, lose more on average, but are also more willing to place larger sized bets. Such behavior is predicted by a model with biased self-assessment, in which investors who believe themselves to be "better-on-average" increase their allocation to an undiversified portfolio. The peanuts hypothesis can therefore forcefully be rejected.

In conclusion, it is found that the top quintile of investors who have the highest active weight loose 3.70% of financial wealth annually, which corresponds to 1.38% of aggregate income within this group. These investors do not only have lower overall wealth and income, but also have the highest aggregate trading losses. Therefore, losses are mainly carried by those who can afford them the least. The latter result have been inferred before from self-reported data by Barber and Odean (2001) and Kumar (2005), and is stressed by Vissing-Jorgensen (2003) and Calvet, Campbell, and Sodini (2006): Private investors may constitute a small part of the stock market, but investment mistakes can potentially have a large impact on individual utility. In the cross-section of individuals, 36% of investors loose more than 1% of their financial wealth due to trading, and 17% of the investors loose more than 5%, measured in annualized terms compared to the own-benchmark. It follows from the concentration of low weighs to the online portfolio in Figure 1 that a large part – 49% of investors – have trading revenues that constitute between plus and minus 1% of financial wealth. Even if almost two-thirds of the investors lose from trading, there are also those who earn sizable amounts. About 8% of the investors gain more than 5%

compared to their benchmark portfolio, measured as a fraction of their financial wealth on an annual basis.

The paper is organized into six sections. Section two explains how trading and portfolio selection is related in a stylized version of the Treynor-Black model. Section three presents the data, section four derives a method of measuring trading revenue and return. Section five presents the results, and section six concludes.

2 A simple portfolio model with overconfidence

Empirical work by Barber and Odean (2000) suggest that individual investors trade far more than can be justified by rational agents within a standard expected utility framework. Active investors earn lower returns due to fees and bid-ask spreads, but also due to unprofitable trading strategies, as found by Grinblatt and Keloharju (2000). Such irrational trading can be explained by overconfidence. In market settings, it is usually enough to model overconfident investors by assuming miscalibration in order to generate trading. More precisely, some investors understate the riskiness of assets as in, e.g., Kyle and Wang (1997), Odean (1998), and Hong, Scheinkman, and Xiong (2005).¹ The psychological literature gives a broader meaning to overconfidence. In the survey of Dunning, Heath, and Suls (2004), they summarize it as follows:

...on average, people say that they are above average in skill (a conclusion that defies statistical possibility), overestimate the likelihood that they will engage in desirable behaviors and achieve favorable outcomes, furnish overly optimistic estimates of when they will complete future projects, and reach judgements with too much confidence.

Therefore, flawed self-assessment is not only the propensity to understate risks, but to hold an overly optimistic view of ones true capabilities. There is some evidence that this distinction of overconfidence is important to explain trading behavior. Using data from

¹Trading can also occur without private information in models of differences in opinion as in, e.g., Harris and Raviv (1993) and Varian (1989). Even if the models in this category generally are silent about the reason for disagreement, all of them share the feature that greater disagreement leads to increased trading.

several UBS/Gallup Investor surveys, Graham, Harvey, and Huang (2005) find that investors who respond that they regard themselves to be competent in the area of investing both trade more frequently and diversify more widely. Glaser and Weber (2004) surveyed online investors and found a robust relation between their measure of the "better-thanaverage" effect and trading activity, but no relation between a traditional measure of miscalibration and trading. In order to formalize the alternative hypothesis to the peanuts effect, and to better understand the different concepts of overconfidence, consider a portfolio problem with a mean-variance investor. With standard quadratic utility, the investor maximize utility by allocating the weight

$$w_{P^*} = \frac{E(R_P^*) - R_F}{\gamma Var(R_P^*)},$$
 (1)

to the risky asset *P*. Ex ante, the investor believe he or she has an ability to outperform the market by $\hat{\alpha}$, on average. Let there be some uncertainty about this ability denoted *T*, and it is independent of the disturbance term *M*. Note that these expectations can be perfectly rational if the investor really is better on average.² We also allow investors to be miscalibrated such that they underweight the true risk of the market, as well as the uncertainty of $\hat{\alpha}$ by a common factor $0 < c \leq 1$. Assuming normality, we have

$$R_M = \mu_M + cM, \ cM \sim N(0, c^2 \sigma_M^2)$$
$$R_T = R_M + \hat{\alpha} + cT, \ cT \sim N(0, c^2 \sigma_T^2)$$

The optimal investment in the trading asset, w_{T^*} , is given by maximizing the Sharperatio of a portfolio of R_M and R_T . The solution is

$$w_{T^*} = \frac{\widehat{\alpha}/\sigma_T^2}{\left(\mu_M - R_F\right)/\sigma_M^2},\tag{2}$$

which is the standard solution to the model of Treynor and Black (1973), as the weight to the traded portfolio is increasing in the appraisal ratio in the numerator. The confidence

²But since investing in the stock market is a zero sum game, this belief also implies that some other investors are below average.

parameter drops out since it scales the numerator and denominator by the same amount.³ Substituting (2) into (1), factorizing, and simplifying the expression gives

$$w_{P^{*}} = \frac{\left(\frac{\hat{\alpha}/\sigma_{T}^{2}}{(\mu_{M}-R_{F})/\sigma_{M}^{2}}\right)\hat{\alpha} + \mu_{M} - R_{F}}{\gamma\left[\left(\frac{\hat{\alpha}/\sigma_{T}^{2}}{(\mu_{M}-R_{F})/\sigma_{M}^{2}}\right)^{2}c^{2}\sigma_{T}^{2} + c^{2}\sigma_{M}^{2}\right]} =$$

$$= \frac{(\mu_{M}-R_{F})^{-1}\sigma_{T}^{-2}(\hat{\alpha}\sigma_{M}^{2} - 2\mu_{M}R_{F}\sigma_{T}^{2} + \mu_{M}^{2}\sigma_{T}^{2} + R_{F}^{2}\sigma_{T}^{2})}{\gamma\left[(\mu_{M}-R_{F})^{-2}\sigma_{T}^{-2}(\hat{\alpha}\sigma_{M}^{2} - 2\mu_{M}R_{F}\sigma_{T}^{2} + \mu_{M}^{2}\sigma_{T}^{2} + R_{F}^{2}\sigma_{T}^{2})c^{2}\sigma_{M}^{2}\right]}{= \frac{\mu_{M}-R_{F}}{\gamma c^{2}\sigma_{M}^{2}}.$$
(3)

Therefore, in the absence of miscalibration, the weight to the risky asset is only a function of risk aversion and the market return. Most notably, it is independent of $\hat{\alpha}$ and σ_T^2 . The intuition for this result is that, due to independence, the allocation to trading scales linearly in mean and variance. The investor allocates more to trading for a higher $\hat{\alpha}$, but keeps the allocation to risky assets at the whole constant. This independence cannot be generalized to arbitrary chosen utility functions, and is not the result to be stressed here. The point is that the choice of an active portfolio directly links to trading, but does not necessarily mean that investors have bigger appetite for risk.

This becomes clear in the case of miscalibration, when c < 1. It is then impossible to discriminate between risk aversion and miscalibration because the parameters are not identified. A miscalibrated investor will have a higher weight to the risky portfolio Pat any level of risk aversion. Note, however, that the weight to the trading portfolio Tis independent of miscalibration. The implication of this stylized model is therefore that turnover is predicted by the weight in the traded portfolio among the set of tradable risky assets, but unrelated to the level of risk aversion and miscalibration. Since the weight to trading is given by the investors' perceived appraisal ratio, it will be correlated with their true stock-picking ability, but also reflect how optimistic they are about their capabilities. In this static model, investors can believe ex-ante that they have such ability, while ex-post, they do not. Such behavior may seem difficult to maintain with updating and

³The fact that the coefficients for miscalibration are the same turns out to be unimportant for the general result below.

realigning expectations. Although not modelled explicitly here, "cognitive dissonance" make people credit themselves for past success and blame external factors for failure (Langer and Roth (1975)). This feature of human behavior could, at least in principle, explain why adjustment is slow.⁴

3 Data

The data were made available by an online broker and cover all transactions since the start in May 1999 up to and including March 2002. The data covers 324,736 transactions in common stocks that are distributed over 16,831 investors who enter sequentially over time.⁵ From this sample, investors are selected that have been active for at least 12 months and from whom there is complete data on wealth and income. The remaining sample is 10,600 investors who made 224,964 common stock transactions distributed over 241,118 investor portfolio months.⁶ The average investor is therefore active approximately 24 months.

In addition to trading data, the sample has been matched to *Statistics Sweden* database with detailed background information of the investors. These data include exact information on investors market value of total portfolio at each year-end. More importantly, all Swedish financial institutions are by law required to report the market value of all individual's financial institutions as well as bank holdings directly to the Swedish Tax Authority. This means that each investor's total portfolio is observable at yearly intervals, and can be matched to those stocks that is held at the particular online broker under study. Furthermore, there is information of housing wealth (taxable), total liabilities, capital insurance, and income. It is also possible to retrieve information if income originates from employment in the financial sector - something that may be indicative of better training in financial decision making. Combined, this allows for a quite detailed analysis of how different investor and portfolio characteristics affect portfolio performance, and in

⁴For an example, see Daniel, Hirshleifer, and Subrahmanyam (1998), who use cognitive dissonance in a dynamic framework to explain slow and asymmetric price adjustment to news.

⁵See Anderson (2004) for a more comprehensive summary of this data.

⁶Total transactions include 120,734 purchases, 82,846 sales, and 21,384 deposits and redemptions of stocks.

particular-detailed controls-when studying turnover performance in the cross-section.

Some features of the data and matching is worth describing in more detail. Income is measured as the first observed year-end disposable income adjusted for net capital gains. Turnover is calculated as the total value of all trades each month divided by two times the portfolio value at the beginning of the month. Finance is an indicator variable if the main source of working income has been earned in the financial sector during the year. Wealth is broken up into three major components: Financial, Real Estate, and Debt. Financial wealth is in turn broken up into bank holdings, money market funds, bonds, stocks, equity and mixed mutual funds, other financial instruments, capital insurance, and other financial wealth. All financial wealth is measured at market values, except for the last component that includes non-listed instruments, private equity, promissory notes, and self-reported values of chattels.⁷ The market value for Real Estate is not observable, but is measured as an adjusted value liable for taxation. In general, the tax value should reflect 75% of the market value, but is sometimes understated in regions of high price increases (i.e. urban areas, or popular areas of recreation). The reported values are conservatively adjusted by multiplying all real estate by the factor 1.33.

Three wealth measures are used. Financial wealth, already defined, Risky assets, and Total wealth. Risky assets includes all financial wealth, except bank holdings and money market funds. This measure of risky wealth is quite wide, but have the advantage that it is clearly defined. Total wealth is Real and Financial assets net of liabilities, but it is assumed that individuals can only borrow on real assets. If market values are indeed understated in spite of the correction, liabilities are assumed to be associated with real estate only, and calculated as the maximum of real estate minus liabilities, and zero.⁸ At the heart of the analysis is the investors active weight. The proxy used here is investors' observed online portfolio value at first year-end, divided by risky assets. Even though real assets also can be regarded as being risky, it is assumed that the part of wealth that is investable

⁷Swedish tax law requires individuals to state the value of private property, such as cars, boats, and jewellery. It is, however, doubtful how close these are to market values since it is virtually impossible to enforce.

⁸This maximum rule was imposed on 3% of investors in sample.

consists only of financial wealth, which is in accordance with the model in section 2. In order to make sure that it is not only individuals that have overall low exposure to the stock and bond market who engage in trading, a separate risk measure is used for control. Trading can also be dependent of risk aversion in a dynamic context, where a given shock to the economy can generate different levels of portfolio rebalancing. A crude measure of risk is calculated as the total holdings of risky financial wealth divided by total wealth. This variable therefore captures the more general propensity for investors to hold risky assets, and the rank correlation with the active weight is but 9%. There are several reasons for this low correlation. Around 46% of the investors in sample had stocks at other accounts at the year of matching, but equally important, around 64% also held an equity mutual fund. In addition, almost 65% of the investors also own real estate, which is an important part of total wealth. In sample, financial wealth constitutes but 34% of total wealth including liabilities, which is typical for Swedish citizens.

The measure of active weight brakes the link between the overall preference for risk, and self-assessed trading ability. It is not necessary that a low active weight implies a preference for lower stock market risk, because risky assets may constitute a large portion of overall wealth. Further, an active weight equal to one means that the individual have all her risky financial wealth invested into the broker account, but this may represent a small part of total wealth if the value of safe assets or real estate is substantial. Investors may trade stocks at other accounts, but the model in section 2 predicts that the allocation and trading decision go hand in hand, such that we should expect a higher concentration of financial wealth allocated to undiversified stock portfolios where turnover is high. It is impossible to discard that individuals with small amounts allocated to their online portfolio also trade extensively in some other assets, or at some other brokerage account where they may choose to concentrate their financial assets. This would, however, only reinforce the main results of this paper, as long as their trading performance is uncorrelated over the accounts they are trading.

Table 1 display the data sorted into quintiles and highest decile with respect to turnover.

Turnover is skewed, where around 15% of investors never trade and the top ten percent of investors turnover around 55% of their portfolio per month (about 6.6 times per year). The average yearly turnover is 113%, which means that the investor buy and sell their portfolio roughly once a year. There is a strong correlation between turnover and active weight. Those in the lowest quintile of turnover, who basically never trade, have about half the active weight as those in the top turnover quintile. This generally rejects the peanuts story as a motivation for trading. Portfolio size is, however, also positively correlated with turnover, which is indicative of that the absolute value of investment also may be a powerful determinant of turnover and that these variables may be interrelated. Diversification is low, where the average investor holds around 3 stocks, and the median investor only 2. Table 1 show that the investors in the lowest quintile of turnover have smaller portfolios and are less diversified. A possible explanation is that these investors refrain from trading due to high trading costs. Income and wealth is highly positively correlated. Investors in the top turnover quintile have somewhat lower income and wealth, but the difference is only statistically significant for income. The difference in risk between low and high turnover investors is significant, where those who trade the most have a larger proportion of their overall wealth invested into stocks. There is a clear and monotonic negative relationship between the amount of females and turnover quintiles. This broadly confirms the results of Barber and Odean (2001), who argue that women are less overconfident compared to men, and therefore also trade less. It is not clear that younger investors trade more than older. The average age in the top decile is about the same as the bottom quintile. The same pattern is observed for those with financial occupation. The representation of this group is more pronounced in the group that trade the least, but also the group that trade the most.

It is worth commenting how the data on wealth, income, and portfolio values relate to Swedish nationals in general. The average portfolio size is skewed with an average at SEK 87,000, the minimum SEK 1,000 and maximum exceeding SEK 19 million. The median stock portfolio in sample is therefore much lower at SEK 18,091. This is, however, approximately what is found for Swedes in general. *Statistics Sweden* report that the median for the whole country is SEK 20,000 and SEK 15,000 at the end of 1999 and 2001. Similarly, diversification is also low for most Swedes. The median Swede only hold one stock. It is difficult to relate income and wealth, as such data is not available for stock holders only. In general, investors in sample have both higher income and wealth compared to Swedes, but is probably a consequence of that stock market participants are wealthier on average. This could also be a reason why women are less represented, since they on average earn lower income.⁹

4 Turnover performance

It is difficult to find a proper benchmark when investors hold undiversified portfolios. The now standard extensions of Markowitz's (1952a) single-index model proposed by Fama and French (1992) and Carhart (1997) may fail to capture specific preferences of, for example, skewness that may be desirable to individual investors.

In the spirit of Grinblatt and Titman (1993), we let the investors instead self-select a benchmark portfolio at the beginning of each month, which is taken as given to reflect the desirable return profile. Ruling out liquidity motives, rational investors with correct expectations of future returns should on average only trade if deviations from the self-selected benchmark is profitable. Even in the presence of "mechanical" motives to trade, such as liquidity and risk management, these costs are expected to be small. If investors trade for liquidity reasons, most investors can either sell or buy a mutual fund (as there are very few funds that have loading and exit fees in Sweden) or lend, alternatively borrow cash. If the investor is constrained, such that this is not applicable, it would still not be rational to trade too frequently at high costs, compared to trading once and store some cash at a bank account. In any of these cases, it is difficult to see why rational investors trade excessively at high costs. In addition, the "constraint motivation" for trading does not square easily with the *positive* correlation between turnover and portfolio size found

⁹The median Swedish woman also had somewhat lower portfolio value compared to men; SEK 13,000 at the end of 1999.

in data.

The approach defining monthly payoffs and returns is as follows. Since the cash account is unobservable on a monthly basis, it is assumed that investors hold unlevereged portfolios and the capital base used when calculating returns is only increased if the transactions involve a net increase in funding. Therefore, it is important to take the exact timing of trades into account. A sale that precedes a purchase need not affect the capital base, but the reverse transaction will. Furthermore, the interest for any cash balance that is either needed for financing or for storing cash must be properly accounted for.¹⁰ A detailed description of how the trading payoff and return is calculated is given below.

4.1 Calculating trading returns

Let $x_{n,i,t}$ be the number of shares of a stock n held by the individual i at the end of month t. A transaction d during month t is denoted by $x_{n,i,d}$, and super-indices B and S indicate whether it is a buy or a sell transaction. Similarly, associated actual purchasing and sales prices including fees are denoted $p_{n,i,d}^B$ and $p_{n,i,d}^S$ for each of these transactions. In what follows, we also need the closing price for stock n on the last day of month t, which is labelled $p_{n,t}^C$. The stock position for individual i at the end of month t is

$$x_{n,i,t} = x_{n,i,t-1} + \sum_{d \in t} \left(x_{n,i,d}^B - x_{n,i,d}^S \right),$$
(4)

which is the position at the beginning of month t plus the sum of buys and sells during the month, hereafter net purchases for short. In what follows, we will impose the restriction that $x_{n,i,t} \ge 0$, meaning that investors are not allowed to have outstanding negative positions at month-end.

¹⁰The approach here is related to that of Linnainmaa (2005) who investigates daytrades, but he only analyzes individual daily stock returns which is different as it avoids the issues involved considering whole portfolios.

4.1.1 Payoffs

Trading, position and total payoffs for each stock and individual are as follows. The position payoff is defined as

$$\Pi_{n,i,t}^{P} = x_{n,i,t-1} \cdot (p_{n,t}^{C} - p_{n,t-1}^{C}),$$
(5)

which is simply the position at the beginning of the month times the change in price. The trading payoff in stock n for individual i during month t is given by

$$\Pi_{n,i,t}^{T} = \sum_{d \in t} p_{n,i,d}^{S} \cdot x_{n,i,d}^{S} - \sum_{d \in t} p_{n,i,d}^{B} \cdot x_{n,i,d}^{B} + \sum_{d \in t} \left(x_{n,i,d}^{B} - x_{n,i,d}^{S} \right) p_{n,t}^{C}.$$
(6)

The first and second component of (6) states the net sales revenue of stock n during month t, which is the value of sells minus buys at actual transacted prices. This value needs to be adjusted if the number of stocks sold exceeds sales, or vice versa. The third component of (6) adjusts payoffs by the value of net purchases that are already accounted for by (5). Deposits of stocks are assumed to be transacted at the beginning of the month and redemptions at the end. Therefore, $x_{n,i,t-1}$ also includes all deposits of stocks made during the month. Investors are allowed to short-sell their stock with these definitions because the summation is invariant to the ordering of purchases and sales. The restriction only means that there must be a positive holding of each stock at the end of the month.¹¹

Total payoff for each investor i in stock n is the sum of trading and position payoff

$$\Pi_{n,i,t} = \Pi_{n,i,t}^{T} + \Pi_{n,i,t}^{P}.$$
(7)

To find the payoff for the whole portfolio, we sum over n to obtain total portfolio payoff for individual i in month t

$$\Pi_{i,t} = \sum_{n} \Pi_{n,i,t} = \sum_{n} \Pi_{n,i,t}^{T} + \sum_{n} \Pi_{n,i,t}^{P}.$$
(8)

¹¹In the sample, this proved to be a minor problem as there were only 34 instances where it was needed to cover open short positions at month's end. This was done by dating the corresponding buy transaction at the beginning of the following month, t + 1, as belonging to t.

4.1.2 Capital components

Similar to payoffs, we distinguish between position and trading capital as follows. Position capital is defined as

$$C_{i,t}^{P} = \sum_{n} \left(x_{n,i,t-1} \cdot p_{n,t-1}^{C} \right),$$
(9)

which is simply the value of all stocks in the portfolio at the beginning of the month.

The amount of capital engaged in trading is determined by sorting each transaction in calendar time. The traded value of any sale or purchase at any day is

$$TV_{i,d} = \left\{ \begin{array}{c} p_{i,d} \cdot x_{i,d}^J \text{ if } J = S \\ -p_{i,d} \cdot x_{i,d}^J \text{ if } J = B \end{array} \right\},$$

such that it represents the revenue of any sales and cost of any purchase. The trade values are ordered during the month from beginning to end for each investor regardless of which stock is traded, and the cash balance is calculated at each point in time. The lowest cumulative cash balance in month t is the minimum amount needed to finance the portfolio without leverage, and is written

$$C_{i,t}^{T} = -\min_{d} \left[\sum_{d \in t} TV_{i,d}, 0 \right],$$
(10)

and is expressed as a positive number since we pick out the largest negative cash balance.

Total capital is the sum of position capital and trading capital,

$$C_{i,t} = C_{i,t}^P + C_{i,t}^T.$$
 (11)

Therefore, the capital base is only increased if trading incurs additional funding. But this is exactly what we want, because the investor who reallocates her investment without using additional funds will have the same capital base.

4.1.3 Excess returns

Excess returns are created as follows. It is assumed that the investor can borrow and deposit cash at the available 30-day T-bill rate, r_{t-1}^F , in order to finance the portfolio. The

interest that is attributable to the position component, $I_{i,t}^P$, is calculated as the cost of borrowing the value of the portfolio at the beginning of the month, i.e the first part of equation (11).

If trading occurs, we seek the net interest paid for trading capital during the month. Interest is calculated for each transaction and summed over the month creating the revenue $I_{i,t}^{T}$ that corresponds to the interest that is attributable to the actual timing of purchases and sales.¹²

The excess return is therefore

$$R_{i,t} = \frac{\prod_{i,t} + I_{i,t}^P + I_{i,t}^T}{C_{i,t} - \min\left[I_{i,t}^T, 0\right]},$$
(12)

where $I_{i,t}^P$ is always 0 or negative and $I_{i,t}^T$ is negative if there is a net cost of financing the monthly transactions. When trading capital is 0 but the investor is net selling, $I_{i,t}^T$ represents the interest earned on investments that is sold out of the portfolio. In this way, timing of the sale is properly accounted for since positive interest is added to the return measure. Both trading capital and $I_{i,t}^T$ can be positive if the investor only draws cash for a short time and for a small amount in comparison to sales revenues in a month.

The interest on trading capital is only added to the capital base if it is negative. This is because it is assumed that interest earned is paid out at the end of the month, but any costs must be covered by capital at the beginning of the month. It therefore ensures that returns are bounded at -1. In the case of no trading, $I_{i,t}^T = 0$, we obtain the familiar definition of excess returns, which is

$$R_{i,t} = \frac{\prod_{i,t} + I_{i,t}^P}{C_{i,t}^P} = r_{i,t} - r_{t-1}^F.$$

4.1.4 Passive returns

The idea of comparing investor performance with their own-benchmark was originally proposed by Grinblatt and Titman (1993). Here, the passive return captures the same

¹²Two assumptions apply: the borrowing and lending rates are the same and the effect of compounding during the month is ignored.

intuition and is defined as

$$R_{i,t}^{P} = \frac{\Pi_{i,t}^{P} - I_{i,t}^{P}}{C_{i,t}},$$
(13)

which is the position payoff divided by total capital corrected for interest. As the ownbenchmark return measures the return of the portfolio since there was no trading during the month, we see that (12) and (13) are exactly the same, because then we have that

$$\Pi_{i,t} = \Pi_{i,t}^P$$

The passive return measure uses total capital as a base. It is therefore assumed that whatever funds used for net investments during the month are invested at the risk-free rate. The investors can only deviate from the benchmark by trading. During the month, investors can move in and out of the market as a whole or switch allocation between stocks. If these tactical changes in risk and reallocations are profitable, investors earn a higher excess return on the traded portfolio than on the static own-benchmark. Trading return is therefore defined

$$R_{i,t}^T = R_{i,t} - R_{i,t}^P, (14)$$

and a the cost of trading per unit of turnover. Turnover cost is

$$TOC_i = \frac{\sum_t (\Pi_{i,t}^T - I_{i,t}^T)}{\sum_t \sum_d TV_{i,d,t}},$$
(15)

and measures trading profit per unit of turnover value.

5 Results

Table 2 summarizes many of the key results of this paper, where the means for the turnover costs and trading returns are partitioned into quintiles of the active weight. Investors with the highest proportion of risky assets invested at the online broker trade more, have larger portfolios, but also lower trading returns. This pattern is clearest for the difference between the fifth and first quintile, which is highly statistically significant. Compared to investors in the bottom quintile of active weight, the top quintile investors loose 18 basis points per month on average. The turnover cost is somewhat U-shaped, but the

difference between the top and bottom quintile of investors is around 0.74%. This means that the flow of money that is traded cost less for investors in the top quintile, but does not compensate enough for their higher turnover. The turnover cost is proportional to the portfolio size, since lower portfolio size is associated with smaller transactions and higher percentage fees.¹³ Investors with the highest active weight have considerably larger portfolios, but size does not explain the average performance *after* fees which is 8 basis points lower compared to the same group. Since the returns are measured to an own-benchmark defined at the beginning of month, the residual is completely due to stock selection and market timing.

The remainder of the analysis of trading performance is conducted in three steps. First, the propensity to trade conditional on the observed characteristics is estimated on the full sample in order to determine the profile of those who trade. This includes taking the marginal probability of those who do not trade into account when calculating the overall effect of investor characteristics on turnover. The second step estimates the relationship between the same characteristics and trading returns, conditional on turnover being positive. The analysis of trading performance is therefore confined to those who actually trade, but concerns the cross-sectional differences in performance of these investors. Finally, the ex-post distribution of trading losses is analyzed.

5.1 Who is trading?

The first step is to determine who is trading, based on the characteristics data. The expectation of average monthly turnover for each individual, TO_i , conditional data \mathbf{X}_i can be written

$$E(TO_i|\mathbf{X}_i) = P(I = 0|\mathbf{X}_i) \cdot 0) + P(I = 1|\mathbf{X}_i) \cdot E(TO_i|\mathbf{X}_i, I = 1)$$
(16)
= $P(I = 1|\mathbf{X}_i) \cdot E(TO_i|\mathbf{X}_i, I = 1),$

where the indicator variable I takes the value one if turnover is observed. Following a version of the corner solution model considered in Wooldridge (2002), assume that if

¹³Anderson (2004) investigate this relationship in more detail.

turnover is observed, it obeys

$$E(TO_i | \mathbf{X}_i, I = 1) = \mathbf{X}_i \beta.$$
(17)

where the error term of the regression is normally distributed. Then the probability that turnover is observed follows a Probit model

$$P(I=1|\mathbf{X}_i) = \Phi(\mathbf{X}_i\lambda).$$
(18)

The models (17) and (18) can be consistently be estimated separately from data. It follows that the marginal effects are

$$\frac{dE(TO_i|\mathbf{X}_i)}{d\mathbf{X}_i} = \beta \Phi(\mathbf{X}_i \lambda) + \mathbf{X}_i \beta \phi(\mathbf{X}_i \lambda) \lambda,$$
(19)

where the first part can be thought of as an "turnover" effect, and the second part a "participation" effect, since a given change in X_i will affect both the probability to trade as well as the magnitude of turnover. Table 3 display the estimation results as well as the marginal effects of the model.

The active weight, portfolio size, and diversification increase the probability to trade. Evaluated at the functional mean, the marginal effects on turnover are about equal around 4%. The positive relation between portfolio size and the decision to trade is not surprising. It is likely that some investors are unwilling to trade in very small portfolios, since trading costs in percentage terms can be high in presence of minimum cost of fees.¹⁴ The probability to trade is significantly decreasing in the level of wealth, risk, female, and age, where overall risk is most important. Investors with high wealth and high stock market risk exposure are less likely to trade, which supports the notion of them being more experienced and better trained in financial decisions.

The OLS estimation generally follows the same pattern, except for diversification and age. Less diversified, as well as younger investors, are less likely to trade, but those who do trade, trade significantly more. There is a strong and positive effect of portfolio size and the active weight. Investors who have a larger share of their financial wealth invested

¹⁴The minimum cost per trade was SEK 89, or roughly USD 10, during the sample period.

at the online account have both a higher probability to trade, as well as higher turnover when they do trade.

The last column of Table 3 shows the effect on turnover of a positive one standard deviation shock to the dependent variable, evaluated at the turnover mean of 9.44%. The most important effect on turnover is portfolio size, which increases turnover by almost 5%, followed by active weight of around 3%. The gender effect is evaluated binary, and shows that the expected turnover of women is 3% lower than that compared to men. The overall effect of risk and wealth on turnover is relatively small compared to the other measured effects.

5.2 Who looses from trading?

So far, it is established that the trading return on average is decreasing in the active weight, and that certain characteristics can be associated with more or less turnover. When controlling for turnover in regressions on the characteristics, it is assumed that the negative effect of turnover is the same for all investors. There is, however, considerable variation in performance, and it is quite possible that turnover does not have the same effect on investor performance conditionally on these variables. Therefore, the characteristic variables are conditioned directly on turnover (TO) in the model

$$R_i^T = a_0 + b_0 \cdot \log(1 + TO_i) + \sum_k b_k \cdot X_{k,i} + \sum_l b_l \cdot \log(1 + TO_i) \cdot X_{l,i} + \varepsilon_i,$$
(20)

where R_i^T denote the average individual trading return, data $X_{k,i} = X_{l,i}$ denote the characteristic variables excluding turnover, and regression coefficients b_k and b_l determines the unconditional and conditional effects of turnover for the investor characteristics. The reason for the (natural) log transformation of turnover is that it fits the data somewhat better. The results are very similar in an untransformed specification. A positive b_k , when b_0 and b_l are excluded, measures the gross effect of the characteristics on performance. This regression disregards that turnover itself vary between investor characteristics, as documented in the previous section. When b_0 is added, controlling for turnover, b_k measures the average performance for investor types. When all coefficients are included in equation (20), b_l is to be interpreted as the marginal impact of trading, conditional on investor type. The coefficients b_k can therefore be thought of as intercepts, and b_l as slopes in the turnover and performance dimension. The point estimates in (20) coincides with OLS, but the variance-covariance matrix is estimated with GMM, using asymptotically robust errors as in White (1980). The results are presented in Table 4.

The regression coefficient for the active weight is significantly negative. The size of the portfolio is a very important determinant for investor performance, since high turnover in small portfolios are associated with higher transaction costs due to fees.¹⁵ When controlling for portfolio size in the second column of Table 4, the point estimate for active weight almost doubles. An increase of 10% in the active weight is associated with a 2.2 basis point drop in monthly trading performance. The negative effect drops, but survives when controlling for other investor characteristics. When turnover is excluded, we neglect that turnover varies systematically over characteristics. The difference between the third and fourth column of Table 4 disentangle these effects. The coefficient for active weight is much lower when controlling for turnover, because investors with high active weights trade more, on average. Therefore, the main channel of underperformance is through increase trading, and not lower average trading ability. Similarly, female investors trade less on average, so the positive effect of 10 basis point higher average performance is almost halved, but still significant at 6 basis points. The effect of diversification is statistically significant, but the economic effect is very small. Investors with one more stock in their portfolio have around 1 basis point less performance. The inclusion of the risk measure ensures that the negative effect of the active weight is unrelated to the overall risky portfolio in relation to total wealth. Rather, higher overall risk-taking is associated with positive trading performance, since a one standard deviation increase in risk improves performance by about 4 basis points. The effect of investors having financial occupation is positive, but insignificant. If wealth and age can proxy for investor experience, these variables give contradicting results. The effect of higher wealth is positive, but age is negative. Both effects are statistically and economically important.

¹⁵As shown by, e.g., Anderson (2004).

A one standard deviation change in these variables represent 10 and 4 basis points in performance. The economically most important effect comes from increased trading alone. A one standard deviation positive shock to turnover above the mean (which corresponds to a turnover level of around 27%) implies an additional 31 basis points in negative trading performance per month–i.e. equally as much as the mean underperformance estimated by the intercept.

The fifth column of Table 4 display the result of the full specification stated in equation (20). The coefficients for active weight is still insignificant, indicating that investors who allocate a large share of their risky wealth to the online account are no better traders, nor worse, than other investors. The magnitudes of the conditional effects are difficult to interpret, so the results for Wealth, Portfolio size, Age, and Financial occupation are highlighted by plotting coefficients for different values of the independent variables in Figure 2A-D. In order to better understand the dispersion of the trading return, these graphs also plot upper and lower quartiles for each of the five turnover quintiles and highest decile, indicating the range for 50% of the observations (crossed, means are circled). All regression coefficients can now be thought of as an "intercept" and a "slope" coefficient in the trading return and turnover dimension. Figure 2A traces out the expected trading return for high (dashed) and low (dotted) wealth investors at the 1st and 3rd quartile of wealth in data. The effect of wealth is mainly better trading performance for higher turnover, since the slope coefficient is high compared to the intercept term. The result indicate that wealthier investors who trade more are better than corresponding low wealth investors. In contrast, investors with higher portfolio size displayed in Figure 2B, seem to have better trading performance in general, which is mainly due to them making larger transactions at lower fees. This is evidenced by the last column in Table 4, where the portfolio size coefficients drops considerably when fees are excluded from the regression. Even if fees also affects the wealth coefficients, the conditional wealth effect is still about half of that when including fees. Therefore, higher wealth is associated with an important positive affect of trading performance that can not only be related to fees. The regression

coefficients of age on performance suggest that young investors are both better traders on average and that trading have less a negative impact on performance, as plotted in Figure 2C. The marginal coefficient for financial occupation is large and strongly significant, but the average effect was insignificant in the previous regression. Figure 2D plots this relation, which implies that it is those with financial occupation who are very active, who have better trading performance on average. This result can be indicative that some of these investors have better information or overall higher ability to execute profitable trades when they do trade. The large difference between financial and non-financial occupation is due to that there are only 326 investors in sample that have employment in the financial sector.

5.3 How much is lost from trading?

The previous section found that investors with portfolios that constitute a large part of financial wealth do not perform better than average. It directly follows that there are investors who loose substantial amounts in relation to their financial wealth. But it has not yet been documented how many these investors are, and how much they loose. The gross trading performance is aggregated for gains and losses separately within the quintiles of active weight and displayed in Table 5. Similarly, financial wealth, total net wealth, and income are also aggregated and net losses expressed as fractions of these measures of investor prosperity. The results from returns carry over to this table, since wealthier investors with lower stakes at the brokerage account both trade less and are better traders on average when they do trade. The sixth row of Table 5 reveals that the investors who are in the lowest quintile of active weight are over three times as wealthy compared to the twenty percent in the top, and possess over ten times as much financial wealth. In addition, the net trading loss is much larger for the fifth than the first quintile. Therefore, the loss incurred by trading is carried by those who can afford them the least. In the fifth quintile sorted on active weight, trading losses represents 3.70% of financial wealth and 1.38% of yearly income. As a comparison, Swedish households with similar income

spend 18.2% of their annual disposable income on recreational activities, on average.¹⁶ For example, general entertainment constitute 2.8%, sports and hobby 1.2%, and recreational travelling 5%, of their total expenditures. Trading losses are therefore far from negligible in this context.

The aggregated results do not display how trading gains and losses are distributed on an individual basis. Figure 3A display the cumulative distribution of net gains normalized by financial wealth and net wealth. The sharp curvature around 0 imply that the trading revenue constitute a small share of wealth for the majority of investors–which is a direct consequence of the distribution for the online portfolio shown in Figure 1. About half, or 49% of the individuals have trading losses and gains representing 1% of their financial wealth. Two thirds of the investors loose from trading, where 36% of them loose more than 1% of financial wealth, and 17% more than 5%. The distribution is skewed, so there are fewer who gains from trading. Still, about 8% of investors gain more than 5% from rebalancing their portfolio to their self-selected benchmark, measured as a share of total financial wealth. The effect is similar, but less sharp when trading revenue is normalized with total net wealth: 20% loose more than 1%, and around 9% more than 5%. Even if fees are an important determinant for returns, Figure 3B shows that these are mainly associated with smaller trading losses. Without fees, 29% of investors loose more than 1% of their financial wealth, compared to 36% when fees are included.

6 Conclusion

Many online investors trade too frequently and most of them loose compared to holding their self-selected benchmark portfolio. This activity is difficult to rationalize with normative financial theory, and attempts have been made to explain this behavior. Most importantly, investors may suffer from overconfidence and illusion of control, as suggested by Barber and Odean (2002), and biased self-assessment as evidenced from Glaser and Weber (2004) and Graham, Harvey, and Huang (2005). They may be sensation-seeking, as proposed by Grinblatt and Keloharju (2005), or simply just untrained in financial de-

¹⁶Matched to the 7th income decile in the 2002 Household Budget Survey, Statistics Sweden.

cision making such that they are unaware of the common traps of stock investment. All the above explanations lean towards the conclusion that investors are uniformed or irrational. A straightforward rational explanation for excessive trading is that investors enjoy trading a small part of their portfolio for their entertainment, as suggested by Conlisk (1993), or they may find it rational to learn about financial markets with small bets before entering with larger investments.

This paper documents that the most active individuals do not gamble with small stakes. When the online portfolio constitutes a large share of risky assets, both the probability to trade increases, and turnover is also increasing in the share of risky assets held at the online account. Furthermore, these investors do not perform better. There is in fact a negative relationship between the share of financial wealth traded and the trading return, measured from a self-selected benchmark. This relation disappears when controlling for turnover, so the main channel of increased underperformance goes through increased trading, and not lower trading ability. High portfolio value and wealth improves trading performance, and wealthier people trade less. This means that the investors who are the least equipped to carry losses, i.e. those with low wealth, are actually those who have the poorest trading performance. In order to assess the importance of the costs across individuals, it is found that two thirds loose from trading, and over one third of the investors loose more than 5% of their financial wealth on an annual basis.

The results do not exclude the possibility that individuals trade for their amusement. If they do, however, the expected utility of gambling must be quite high for many investors. More over, there is little reason for allocating a large share of financial wealth to this activity if it is trading itself that is rewarding, and there may be other games that are less expensive to play in order to reach the same level of satisfaction. A simpler, and very plausible alternative explanation forwarded here is that investors who believe themselves to be better on average engage more heavily in trading. A slightly modified Treynor-Black portfolio allocation model predicts that this relation can be independent of the overall level of financial risk-taking and how much the individual under-weights the true riskiness of the stock market. The empirical evidence supports this proposition, as the active weight is one of the strongest predictors of turnover. In particular, there is a very weak link between overall financial risk-taking and trading frequency. The evidence from the performance regressions suggest that biased self-assessment is mainly an idiosyncratic phenomena. Investors who tilt their risky portfolio to stocks at their online portfolio trade more, but are no better than other investors.

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Table 1: Mean statistics sorted on turnover

The 10,600 investors are sorted into quintiles (and tenth decile) based on turnover, defined as the sum of monthly purchases and sales divided by two times portfolio value. Portfolio size is the value of the portfolio at the end of the first month of trading, which is also when Age and the number of different stocks held, Diversification, is determined. All other variables are defined at first observed year-end. The active weight is the online portfolio value divided total risky financial wealth. Income is disposable income net of capital gains. Wealth includes financial wealth and the maximum of adjusted housing wealth net of liabilities. Risk is measured as risky assets divided by wealth. Females and Finance measures the frequency of women and those who earned income from financial occupation. All reported values are means, unless stated otherwise. Under the sample period, USD 1 corresponds to about SEK 9.

| | Turnover quinitles | | | | | Decile | Diff. | Test- | |
|-------------------------|--------------------|---------|---------|---------|-------------|---------|---------|--------------------|-----------------------|
| | 1 (Low) | 2 | 3 | 4 | 5 (High) | 10 | All | Q5-Q1 ¹ | statstic ² |
| Turnover, % | 0.06 | 1.49 | 3.56 | 7.25 | 34.86 | 54.84 | 9.44 | 34.80 | 41.97*** |
| Active weight, % | 32.62 | 40.84 | 43.24 | 48.80 | 58.62 | 64.29 | 44.82 | 26.00 | 22.77*** |
| Portfolio size, SEK | 60,272 | 91,217 | 73,821 | 72,286 | 133,321 | 175,795 | 86,183 | 73,049 | 6.74*** |
| Diversification, stocks | 2.18 | 3.25 | 3.27 | 3.29 | 2.99 | 2.87 | 3.00 | 0.81 | 11.41*** |
| Income, SEK (median) | 336,397 | 321,395 | 316,357 | 307,919 | 296,025 | 301,491 | 315,249 | -49,772 | -3.60*** |
| Wealth, SEK (median) | 761,931 | 658,746 | 674,697 | 589,036 | 654,482 | 627,020 | 663,379 | -50,165 | -0.52 |
| Risk, % (median) | 23.14 | 26.93 | 25.66 | 24.71 | 29.13 | 30.02 | 25.97 | 3.39 | 3.02*** |
| Females, % | 23.35 | 20.42 | 20.05 | 14.43 | 11.89 | 11.13 | 18.03 | -11.46 | -9.82*** |
| Age, yrs | 39.21 | 37.97 | 38.15 | 37.55 | 38.36 | 39.27 | 38.25 | -0.85 | 2.39** |
| Finance, % | 3.40 | 2.12 | 3.16 | 3.02 | 3.68 | 3.40 | 3.08 | 0.28 | -0.50 |

1) Difference in means between first and fifth quintile. 2) Test of difference in means (or proportions where applicable). Asterisks ***, **, and * denote significance on the 1%, 5%, and 10% percent level.

Table 2: Trading returns and turnover costs

Investors are sorted into quintiles of active weight, which is the online portfolio value divided by total risky assets at first year-end. The rows display the mean trading return, with and without fees, the turnover cost defined in the main text, average turnover, and portfolio size.

| Variable | | Quintil | | Difference | | | |
|-------------------|-----------------------|------------------------|-----------------------|-------------------------|-------------------------|-----------------------|-----------------------|
| means | 1 (Low) | 2 | 3 | 4 | 5 (High) | All | Q5-Q1 |
| Active weight, % | 1.96 | 11.36 | 35.00 | 75.93 | 99.87 | 44.82 | 97.91 |
| Trading return, % | -0.23 ^{***} | -0.23 ^{****} | -0.21 ^{****} | -0.25 ^{***} | -0.41 ^{***} | -0.26 ^{****} | -0.18 ^{****} |
| | (-11.13) | (-11.61) | (-10.48) | (-11.16) | (-12.61) | (-25.20) | (-4.61) |
| Trading return | -0.07 ^{***} | -0.07 ^{***} | -0.04 ^{***} | -0.07 ^{***} | -0.15 ^{***} | -0.08 ^{***} | -0.08 ^{**} |
| (w/o fees), % | (-3.37) | (-3.76) | (-2.59) | (-3.58) | (-5.11) | (-8.48) | (-2.36) |
| Turnover | -3.12 ^{***} | -2.80 ^{***} | -2.23 ^{***} | -1.51 ^{***} | -2.38 ^{***} | -2.41 ^{***} | 0.74 ^{**} |
| cost, % | (-10.22) | (-10.35) | (-10.58) | (-9.54) | (-11.68) | (-22.83) | (2.01) |
| Turnover, % | 4.59 ^{***} | 6.86 ^{***} | 8.17 ^{***} | 13.28 ^{***} | 14.33 ^{***} | 9.44 ^{***} | 9.74 ^{***} |
| | (22.57) | (20.34) | (21.19) | (23.85) | (21.67) | (45.37) | (14.08) |
| Portfolio size, | 32,165 ^{***} | 46,694 ^{****} | 91,909 ^{***} | 156,780 ^{****} | 103,368 ^{****} | 86,183 ^{***} | 71.203 ^{***} |
| SEK | (7.19) | (13.53) | (8.38) | (15.83) | (11.75) | (23.42) | (7.26) |

Significance of a t-test (test statistics within parenthesis) are marked by ***, **, and *, indicating rejection at the 1%, 5%, and 10% level.

Table 3: Estimates of the determinants of turnover

The table display the parameters of a probit-estimation on the whole sample, and associated slope coefficients calculated at the functional mean. The OLS regression is specified over the 9,053 investors with non-zero turnover, defined as the sum of monthly purchases and sales divided by two times portfolio value. Portfolio size is the value of the portfolio at the end of the first month of trading, which is also when Age and the number of stocks held, Diversification, is determined. All other variables are defined at first year-end. Active weight is the online portfolio value divided by total risky financial assets. Income is disposable income without realized net capital gains. Wealth includes financial wealth and the maximum of adjusted housing wealth net of liabilities. Risk is measured as the value of risky assets divided by total wealth. Female and Finance are indicator variables for women or if income has been earned from financial occupation. The marginal effects for the combined model is decomposed into the marginal effect on turnover and participation. The last column reports the effect on turnover of a one standard deviation shock to the independent variable. Intercepts are suppressed.

| Model | Probit 10,600 obs. | | OLS 9,053 obs. | Marginal effects ¹ | | | Turnover, one std. dev. |
|-----------------------|----------------------------------|--------------------|-----------------------------------|-------------------------------|---------|---------------|-------------------------|
| Dependent var: | Trading (I/0) | Slope ¹ | Turnover | Total | Trading | Participation | shock to ² |
| Active weight | 0.210 ^{***} (3.80) | 0.035 | 8.169 ^{***} (8.67) | 7.776 | 7.402 | 0.374 | 2.978 |
| Log Portfolio Size | 0.212 ^{***} (13.92) | 0.036 | 3.216 ^{****} (11.68) | 3.293 | 2.914 | 0.379 | 4.888 |
| Diversification | 0.255 ^{***} (19.02) | 0.043 | -1.145 ^{****} (-6.19) | -0.582 | -1.037 | 0.455 | -1.537 |
| Log Wealth | -0.067 ^{***} (-4.60) | -0.011 | -0.236 (-1.02) | -0.333 | -0.214 | -0.119 | -0.615 |
| Risk | -0.105 (-1.64) | -0.018 | 1.916 [*] (1.73) | 1.549 | 1.737 | -0.188 | 0.564 |
| Female | -0.146 ^{***} (-3.57) | -0.024 | -3.228 ^{****} (-6.67) | -3.185 | -2.925 | -0.260 | -3.185 |
| Log Age | -0.100 [*] (-1.68) | -0.017 | 5.747 ^{***} (6.29) | 5.029 | 5.208 | -0.179 | 1.538 |
| Finance | -0.115 (-1.26) | -0.019 | 1.986 (0.96) | 1.593 | 1.799 | -0.206 | 1.593 |
| (Quasi) R-squared | 0.139 | | 0.077 | | | | |

Reported t-statistics within parenthesis are based on Whites heteroscedastic standard errors. Asterisks ^{*}, ^{**}, and ^{***} denote significance on 1%, 5%, and 10% level. 1) Marginal effects evaluated at the regression mean. 2) Estimated effect to turnover of one standard deviation shock to the independent variable, except for "Female" and "Finance" evaluated for binary values.

Table 4: Estimates of the determinants of trading return

The table display the linear regression coefficients from various specifications with the trading return as the dependent variable. Turnover is defined as the sum of monthly purchases and sales divided by two times portfolio value. Portfolio size is the value of the portfolio at the end of the first month of trading, which is also when Age and the number of different stocks held, Diversification, is determined. All other variables are defined at first year-end. The active weight is the online portfolio value divided by total value risky financial assets. Income is disposable income net of capital gains. Wealth includes financial wealth and the maximum of adjusted housing wealth minus liabilities. Risk is measured as risky financial wealth divided by wealth. Female and Finance are indicator variables for women or if income has been earned from financial occupation. The first five columns regress the trading return including fees directly on the independent variables, where the fifth column also condition them on turnover. The previous analysis is repeated in the last column, but with turnover return excluding fees as the dependent variable. All independent variables have been centralized.

| Dependent variable | | | Frading return | | | Excl. fees |
|---------------------|------------|------------|----------------|---------------|---------------|--------------|
| Intercept | -0.310**** | -0.310**** | -0.310**** | -0.310*** | -0.326*** | -0.0844** |
| Intercept | (-25.35) | (-25.57) | (-25.65) | (-26.11) | (-22.16) | (-6.33) |
| log (1+Turnover), | | | | -1.575*** | -1.965*** | -0.537** |
| LTO | - | - | - | (-7.92) | (-8.21) | (-2.53) |
| Active weight | -0.122*** | -0.221*** | -0.118** | -0.023 | -0.014 | -0.015 |
| Active weight | (-3.40) | (-5.81) | (-2.60) | (-0.54) | (-0.32) | (-0.38) |
| LTO*Active w. | _ | _ | _ | _ | 0.428 | -0.486 |
| LIO Active w. | - | - | _ | - | (0.86) | (-1.13) |
| Log Portfolio Size | _ | 0.105*** | 0.078^{***} | 0.113*** | 0.119*** | 0.030*** |
| Log I ortiono Size | | (12.61) | (7.04) | (9.84) | (11.34) | (3.08) |
| LTO* Log Portfolio | _ | | _ | _ | 0.335*** | 0.070 |
| Size | | | | _ | (2.99) | (0.68) |
| Diversification | _ | | -0.001 | -0.014** | -0.017*** | -0.006* |
| Diversification | | | (-0.21) | (-2.47) | (-4.86) | (-1.82) |
| LTO*Diversification | _ | | _ | _ | 0.012 | 0.072^* |
| ETO Diversification | | | | _ | (0.26) | (1.79) |
| Log Wealth | _ | | 0.065*** | 0.065^{***} | 0.062*** | 0.025^{**} |
| Log Would | | | (4.43) | (4.54) | (4.56) | (2.05) |
| LTO*Log Wealth | - | | _ | _ | 0.688^{***} | 0.322^* |
| ETO EOS Would | | | | | (3.03) | (1.79) |
| Risk | _ | | 0.104** | 0.140^{***} | 0.131*** | 0.034 |
| MBR | | | (2.10) | (2.75) | (2.84) | (0.81) |
| LTO*Risk | _ | | _ | _ | 1.262^{*} | 0.434 |
| LIO Risk | | | | | (1.90) | (0.86) |
| Female | _ | | 0.100^{***} | 0.063** | 0.065^{*} | 0.061^* |
| 1 onnaio | | | (3.54) | (2.24) | (1.84) | (2.00) |
| LTO*Female | - | | - | - | 0.283 | 0.787^{*} |
| 210 10000 | | | de de de | dist | (0.50) | (1.75) |
| Log Age | - | | -0.181*** | -0.117** | -0.123** | -0.104** |
| 88- | | | (-3.65) | (-2.37) | (-2.57) | (-2.40) |
| LTO*Log Age | - | | - | - | -2.398*** | -2.108*** |
| 210 2081.90 | | | | | (-3.44) | (-3.86) |
| Finance | _ | | 0.002 | 0.019 | -0.014 | 0.016 |
| | | | (0.04) | (0.26) | (-0.22) | (0.26) |
| LTO*Finance | _ | | - | - | 1.538*** | 1.229** |
| | | | | | (2.95) | (2.55) |
| R-squared | 0.016 | 0.019 | 0.024 | 0.059 | 0.086 | 0.027 |

Reported t-statistics within parenthesis are based on Whites heteroscedastic standard errors. Asterisks ***, **, and * denote significance on 1%, 5%, and 10% level.

Table 5: Aggregate trading losses

Then 10,600 investors in sample are sorted into quintiles and top decile of active weight, which is the observed portfolio value observed at first year-end divided by total financial wealth. The net trading payoff for each investor is aggregated into total losses and gains for each of the two groups. The four bottom rows display and normalizes net gains with total financial wealth, total wealth, and income net of capital gains for each investor group. Values are in thousands of Swedish crowns (tSEK), where USD 1 roughly corresponds to SEK 9.

| Aggregate | | | | | | |
|-------------------------------|-----------|-----------|-----------|-----------|-----------|------------|
| trading revenue | 1 | 2 | 3 | 4 | 5 | All |
| and wealth | (Low) | | | | (High) | |
| Total losses, tSEK | -4,773 | -6,495 | -8,740 | -25,258 | -17,446 | -62,712 |
| Total gains, tSEK | 3,260 | 4,574 | 7,395 | 15,950 | 8,047 | 39,226 |
| Net gains, tSEK | -1,513 | -1,921 | -1,345 | -9,308 | -9,399 | -23,486 |
| Financial wealth, tSEK | 2,721,510 | 715,594 | 529,765 | 542,274 | 254,310 | 4,763,453 |
| Net gains / fin. wealth, % | -0.06 | -0.27 | -0.25 | -1.72 | -3.70 | -0.49 |
| Wealth, tSEK | 5,503,150 | 2,403,157 | 2,162,958 | 2,056,789 | 1,537,862 | 13,663,916 |
| Net gains / wealth, % | -0.03 | -0.08 | -0.06 | -0.45 | -0.61 | -0.17 |
| Income, tSEK | 921,176 | 768,121 | 763,074 | 713,012 | 678,759 | 3,844,142 |
| Net gains / income, % | -0.16 | -0.25 | -0.18 | -1.31 | -1.38 | -0.61 |

Figure 1: The online portfolio weight

The cumulative frequency distribution of the online portfolio weight is plotted for the 10,600 investors in sample. The online portfolio is defined as portfolio value at first, observable year-end, divided by either total market value of risky assets or total financial wealth.

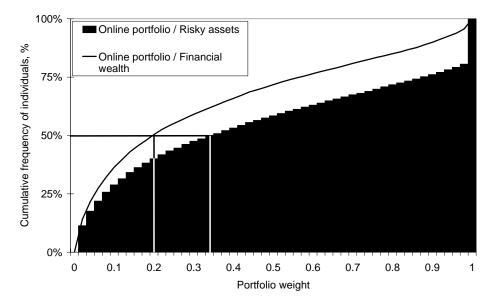


Figure 2: Regression slopes conditional on turnover

Figures 2A-D shows regression slopes from numerical experiments when manipulating the independent variables. Figures 2A shows the effect of investors with wealth at upper and lower quartiles in sample. Figures 2B and 2C repeat the analysis for Portfolio size and Age. Figure 2D shows the expected trading performance for investors with and without Financial occupation. Circles trace out the mean for the trading return quintiles and top decile, where crosses shows the first and third return quartile for each group.

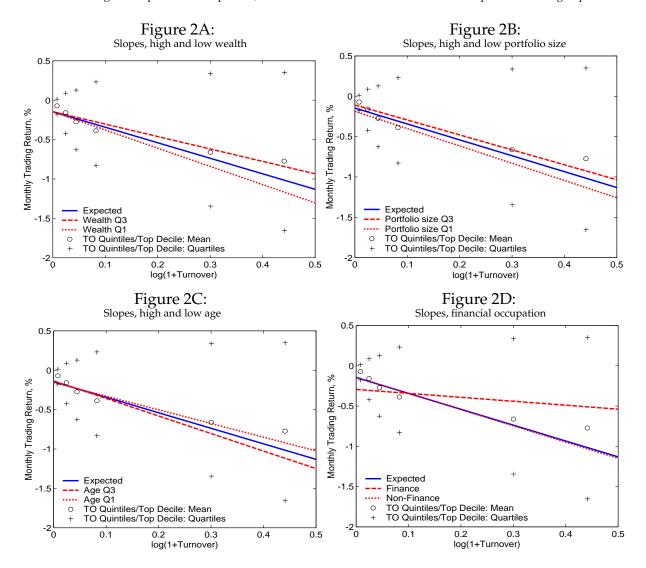


Figure 3: Cumulative frequency distributions of net gains as a share of wealth

Figure 3A depicts the cumulative frequency distribution for the net annualized gains of 10,600 investors in sample, measured as a share of financial wealth as well as total wealth. Figure 3B display net annualized gains divided by financial wealth with and without fees.

